



## Modeling and Estimating the Uplift Force of Gravity Dams Using Finite Element and Artificial Neural Network Whale Optimization Algorithm Methods

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**ABSTRACT:** The correct identification of the uplift force plays an important role in the stability analysis of gravity dams. Therefore, it is very important to estimate it accurately. For this purpose, a numerical model of the foundation of a gravity dam of the Guangzhao, China was made using finite element method. After simulation, the uplift force values were obtained in different positions of drainage. Require experience, the timing of calculations and the accurate determination of the boundary conditions in numerical models, have caused to the development of the tendency to use intelligent models. For this purpose, in addition to the Artificial Neural Network model (ANN) with three-layer that consists of 4 input neurons, 1 hidden layer (with 8 neurons), and 1 output neurons, a new hybrid model of Artificial Neural Network-Whale Optimization Algorithm (ANN-WOA), was developed. The ratio of the parameters of the distance of the drain row from upstream dam, the distance from the center to center of drains, the drain diameter and the water surface upstream of the reservoir dam respect to the width of the dam foundation as input and relative uplift force were considered as output. The values of  $R^2$ , RMSE and RE% for the ANN-WOA model, were 0.998, 0.021 and 3.3%, respectively, and for the ANN model were 0.995, 0.261 and 4.67% respectively, that indicate the higher accuracy of the ANN-WOA model in the estimation of the uplift force than the ANN. In addition, the density plot box and the violin plot indicate that the point density and the probability distribution estimated data with the ANN-WOA model is very similar to that the data obtained from the numerical simulation compared with the ANN model.

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## 1. INTRODUCTION

Seepage from the dams and the resulting increase in uplift force is considered as one of the most important factors in the destruction of dams. All dams and structures associated with water storage are subjected to water flowing from the foundation, sides and sometimes their bodies. Thus, the water in the reservoir of the dam, at any moment, tends to seepage from the seam and the gap at the junction of the dam and the pores in the soil. The water flows from below the dam and appears in the downstream. The force from the bottom upwards to the dam body, is sometimes referred to as uplift force. The uplift force sometimes is so high that it causes the overturning of the dam. Therefore, it is necessary to make projections and logistics in design, in order to reduce the amount of this force in design of the dam. This may be done by installing a drainage gallery in the dam body. Inside the drainage gallery, drainage wells collect seepage water from the body of the dam, and especially from the dam foundation.

A theoretical solution based on seepage theory was presented by Chawla et al. (1990) to determine optimal location of the drainage gallery system with equally spaced drains of uniform diameter of gravity dams. The optimal

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location of the drainage gallery was selected for state that uplift force is minimum [1]. Optimum location for vertical drains in gravity dams was investigated by Nourani et al. (2016). Results showed that the optimum location of the vertical drain in drainage gallery system is not fixed, therefore, for each dam, the optimal location of the vertical drain will be determined by considering the effective factors [2]. Salmasi et al. (2017) investigated the reduction of uplift forces by longitudinal drains with underlined canals. The investigation generates sufficient data for typical 2D canal cross-sections by numerically solving a wide range of configurations using a provision of drain pipes. The generated data comprise the correlation between uplift forces and the various configuration parameters in terms of effects of position of the drain pipes, their size and hydraulic factors, such as the effect of phreatic surface [3].

In this study, to estimate the total uplift force in gravity dams, a numerical model of the gravity dam is introduced using finite element method. This numerical simulation includes drainage system under the dam foundation. The diameter of drains pipe, their location from the dam heel and the distance among drains center are variables in this study. After numerical simulation, the relative total uplift force values is estimated using ANN model. Then a new hybrid model of



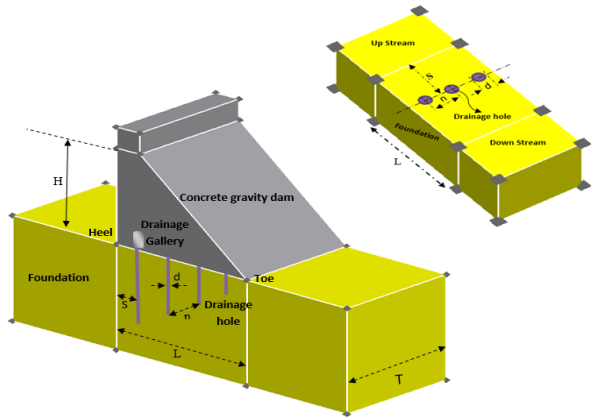


Fig. 1. Illustration the drain holes row of drainage gallery system in the gravity dam

Artificial Neural Network-Whale Optimization Algorithm (ANN-WOA), is developed and the accuracy of these intelligence models will be compared. Application of the ANN-WOA model in prediction of the uplift force in gravity dams was not found in the literature review.

## 2. METHODOLOGY

### 2.1 Governing Equations

The general equation of flow in porous media is the Darcy's equation, which this equation combines with the continuity equation of flow and convert to Richard's equation, which is a partial differential equation describing seepage performance. The general governing differential equation for two-dimensional (2D) seepage can be expressed as:

$$\frac{\partial}{\partial x} \left( k_x \frac{\partial h}{\partial x} \right) + \frac{\partial}{\partial y} \left( k_y \frac{\partial h}{\partial y} \right) + Q = \frac{\partial \theta}{\partial t} \quad (1)$$

where  $h$  the total head,  $Q$  is the applied boundary flux (m/s),  $\theta$  is the volumetric water content ( $m^3/m^3$ ),  $k_x$  is the hydraulic conductivity in the  $x$ -direction (m/s),  $k_y$  is the hydraulic conductivity in the  $y$ -direction (m/s) and  $t$  is time. The above equation (Eq.1) in steady state condition changes as follows:

$$\frac{\partial}{\partial x} \left( k_x \frac{\partial h}{\partial x} \right) + \frac{\partial}{\partial y} \left( k_y \frac{\partial h}{\partial y} \right) + Q = 0 \quad (2)$$

In conditions that the porous media is homogeneous and isotropic ( $k_x=k_y$ ) and input and output flow is zero ( $Q=0$ ) the equation 2 is simplified in the form of equation 3, which is known as the Laplace's equation.

$$\frac{\partial^2 h}{\partial x^2} + \frac{\partial^2 h}{\partial y^2} = 0 \Rightarrow \nabla^2 h = 0 \quad (3)$$

The SEEP/W software (a part of Geo-Studio software) uses the finite element method (FEM) to solve the governing (Laplace) seepage equation regarding specified boundary conditions [4].

### 2.2 Numerical Simulation / Finite Element Method (FEM)

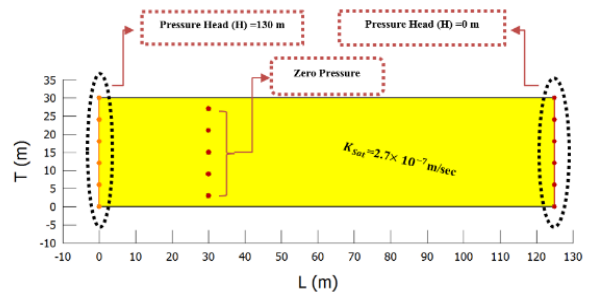


Fig. 2. Plan view foundation of dam with 5 drains, with specified boundary conditions ( $s=30$  m,  $d=0.15$  m,  $n=6$  m,  $H=130$  m)

In this study, a gravity dam with the dimensions shown in Fig.1 is considered. It should be noted that in this study, the width of the floor of the dam ( $L$ ) and the length of the dam ( $T$ ) to the order of 125 and 30 meters is considered.

The uplift force in gravity dams is dependent of the function of the vertical drains of the drainage gallery. The effective factors are the diameter drain ( $d$ ), the distance from the center to center the drains ( $n$ ), the distance drain row from heel of dam ( $s$ ), and water surface in upstream of the reservoir ( $H$ ). In addition of simulation the foundation of gravity dam in state of without drainage gallery, 12 other models including vertical drains are located inside the drainage gallery in different diameters ( $d$ ) of 0.05, 0.10 and 0.15 meters, each of which in 4 modes with distance ( $n$ ) of 3, 4, 5 and 6 meters. Also, the effect of the distance drain row from heel of dam ( $s$ ) has been considered. For this purpose, the distance of drains row from upstream of dam in 12 different positions are 0, 5, 10, 15, 20, 25, 30, 40, 60, 80, 100 and 125 meters. The aforementioned conditions have been used for two states of water surface upstream of the reservoir dam ( $H=168$  and  $130$  m). Thus that the effect of water surface level of the reservoir also is investigated. Fig.1 indicates a schematic view of the location of the drains in the drainage gallery and the parameters in this study. Depending on the conditions of the present study, the plan view of SEEP/W software is used to simulate dam foundation along with the vertical drainages. Fig. 2 shows the plan view foundation of dam in software media in state of that  $s, d, n$  and  $H$  is equals 30, 0.15, 6 and 130 meters respectively.

For numerical simulation, the boundary conditions at the upstream and downstream of the gravity dam are equal to the water surface level at the reservoir and tail water in the form of a pressure heads. In this study the upstream water level variation is 168 and 130 meter, while the water level in downstream is set to zero. For setting the boundary condition, Pressure head in upstream is 168 and 130 meters. Also the boundary conditions at the vertical drains, was considered as zero pressure. Since all the analyses are for a steady state condition, volumetric water content not required. The foundation of dam material was considered homogeneous and isotropic within a saturated permeability of  $K_{sat}=2.7E-07$  meters per second (m/s) (Fig. 2).

### 2.3 ANN and ANN-WOA Modelling

In this research, two models of ANN and ANN-WOA are used to estimate the relative total uplift force ( $U_d/U_o$ ) using

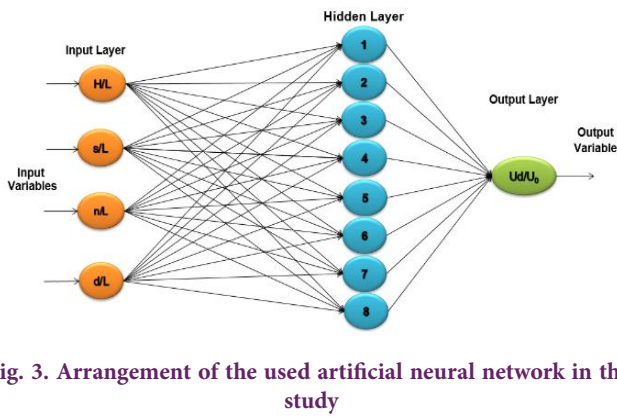


Fig. 3. Arrangement of the used artificial neural network in this study

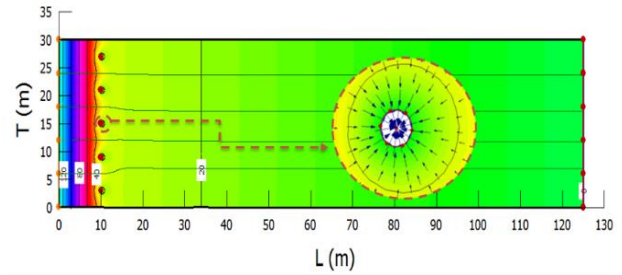


Fig. 4. Potential contour lines, flow lines and velocity vectors at foundation of the gravity dam with vertical drain ( $s=10$  m,  $d=0.015$  m,  $n=6$  m,  $H=130$  m)

Table 1. values of the parameters used in the WOA method

Parameters	$L$	$P$	Population size	Maximum iteration	Hidden layer
Range in this study	0.37	0.65	30	50	8

4-Input variables  $H/L$ ,  $d/L$ ,  $n/L$  and  $s/L$ . The generated data are available after the several numerical simulations using finite element method. In both models (ANN and ANN-WOA), the non-dimensional parameters  $H/L$ ,  $d/L$ ,  $n/L$  and  $s/L$  are as the input variables and the non-dimensional parameter  $U_d/U_o$  (relative total uplift force) is used as output variable. Each set of data consists of 288 dataset. In both models, 70% of the dataset (200 data) is used for the training and 30% of the dataset (88 data) is used for the testing phase. It should be noted that a code was written in the Wolfram Mathematica software so that the dataset are randomly selected for each two training and testing period for several times. Then the desired model was selected based on the best values for determination coefficient ( $R^2$ ) and the root mean square error (RMSE). After 50 repetitions of the above-mentioned random selection criteria in the Wolfram Mathematica software, the best conditions for  $R^2$  and RMSE were selected ( $R^2 = 0.995$  and  $RMSE = 0.0223$ ). Fig. 3 shows a three-layered structure used in this study that consists of (i) input layer, (ii) hidden layer, and (iii) output layer. The independent variables in input layer are:  $s/L$ ,  $n/L$ ,  $d/L$  and  $H/L$ . The dependent variable used as output is  $U_d/U_o$ . The optimum network architecture was defined as 4-8-1 that include 4 neurons for input, 1 hidden layer with 8 neurons and 1 output neuron. In addition, the sigmoid tangent function for the input layer and the linear function for the output layer was selected using the Levenberg Marquard Algorithm (LMA) with repeating 200. In this study, for the WOA method the values of  $P$  and  $L$  were 0.65 and 0.37, respectively and also population size and maximum iteration were 30 and 50, respectively. Optimum number of neurons in hidden layer was 8 (Table 1).

### 3. RESULTS AND DISCUSSION

After numerical simulation using FEM, the pore water

pressure is calculated in each point in the porous medium of soil in dam foundation. Fig. 4 shows the potential contours, flow lines and velocity vectors in state of that  $s$ ,  $d$ ,  $n$  and  $H$  is equals 10, 0.10, 6 and 130 meters, respectively

The comparison of the observed and estimated data of  $U_d/U_o$  by ANN and ANN-WOA models in testing period are shown in Figs. 5 and 6 in the form of scatter plots. It can be seen from the linear line fit equations and  $R^2$  values in scatter plots that the ANN-WOA estimates are closer to the observed values than the ANN model. Thus ANN-WOA performs much better than the ANN model and therefore has a very high accuracy in estimating of the parameter  $U_d/U_o$ .

In this study, a model was developed for estimating the relative total uplift force,  $U_d/U_o$  in gravity dams using ANN and ANN-WOA. Statistical values consist of ( $R^2$ , RMSE and RE%) of the training and testing dataset period for ANN and ANN-WOA methods are given in Table 2. Statistical criteria testing dataset show that ANN-WOA has better results than ANN. Therefore, the ANN-WOA model provides very similar results to the results finite element method in estimating of  $U_d/U_o$ .

Results of the numerical simulations in the present study have been validated by comparison Chawla et al. (1990)'s analytical method for the same conditions. In Table 3, the results of Chawla et al. (1990), numerical model using SEEP/W software, ANN model and ANN-WOA model for conditions of  $d/L = 0.0004$ ;  $n/L = 0.048$  and  $H/L = 1.344$  for two states of  $s/L = 0.24$  and  $0.32$  have been shown.

### 4. CONCLUSION

In this research, the two models of ANN and ANN-WOA have been used to estimate the total uplift force in gravity dams. The relative total uplift force ( $U_d/U_o$ ) under the gravity dam in contact with foundation was generated using numerical model

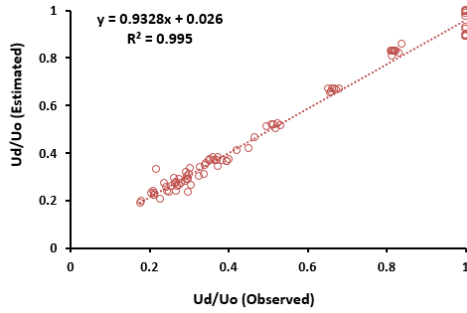


Fig. 5. Scatter plot of the observed and estimated data for testing period using ANN model

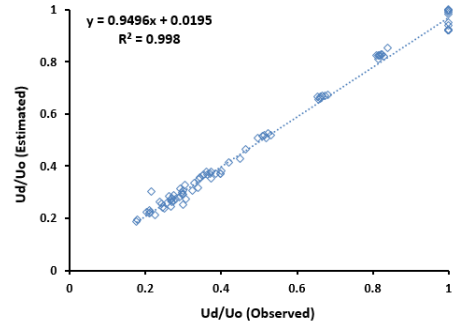


Fig. 6. Scatter plot of the observed and estimated data for testing period using ANN-WOA model

Table 2. Statistical values of training and testing period for ANN-WOA and ANN models

	Test data			Train data		
	R <sup>2</sup>	RMSE	RE%	R <sup>2</sup>	RMSE	RE%
ANN	0.955	0.0223	4.67	0.994	0.0236	<b>3.4</b>
ANN-WOA	0.998	0.021	3.50	0.991	0.0177	<b>2.6</b>

SEEP/W. Then, the estimated values of  $U_d/U_o$  were compared with the two models named ANN-WOA and ANN. These comparisons are based on three evaluation criteria, i.e., R<sup>2</sup>, RMSE and RE%. It should be noted that the ANN model was performed using a code in the Wolfram Mathematica software with random sample selections. Total number of the data was 288 and 30% (88 data) was selected as testing phase and 70% (200 data) was selected as training phase. After repeated multiple random choices from all available data, the data for the conditions with the highest R<sup>2</sup> and lowest RMSE for the estimated process was used in the ANN model. The results of this study showed that both intelligent models have reasonable accuracy in estimating of the relative total uplift force ( $U_d/U_o$ ). The values of R<sup>2</sup>, RMSE and RE% for ANN-WOA model were 0.998, 0.021 and 3.3% respectively. These values for ANN were 0.995, 0.022, and 4.67% respectively. Both of the ANN-WOA and ANN models were successful in prediction of  $U_d/U_o$ .

Table 3. Comparison of ANN-WOA, ANN, SEEP/W and Chawla et al. (1990) results for testing phase

Method	(s/L=0.024)	(s/L=0.032)
	$U_d/U_o$	$U_d/U_o$
Chawla et al. (1990)	0.350	0.391
SEEP/W	0.369	0.420
ANN-WOA	0.371	0.414
ANN	0.372	0.411

$U_o$ . The data density diagrams and the iolin diagram were also obtained and was observed that the dispersion and probability distribution of the ANN-WOA model is resembled with the results of the numerical simulation.

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